

Section 8 – 5C: **Testing a Claim About the Population Standard Deviation**
Examples

Example 1 (One Tail Right Tail Test)

The Folsom City Housing Office reports that the average rent for a two bedroom apartment in Folsom has an average cost of \$ 1200 with a standard deviation of \$ 250. An advocate for renters claims that the standard deviation is much larger than the \$ 250 that the Housing Office reported. The city decides to conduct a review of rents in Folsom. They take **a random sample of 51** two bedroom apartments and find that the **average rent is \$1225** with a **standard deviation of \$ 315**. Test the claim at a **.01 significance level** that the standard deviation in the rent of two bedroom apartments is **more than \$ 250**. Assume that **the population is normal**.

$H_0: \sigma = 250$

Sample Standard Deviation: $s_x = 315$

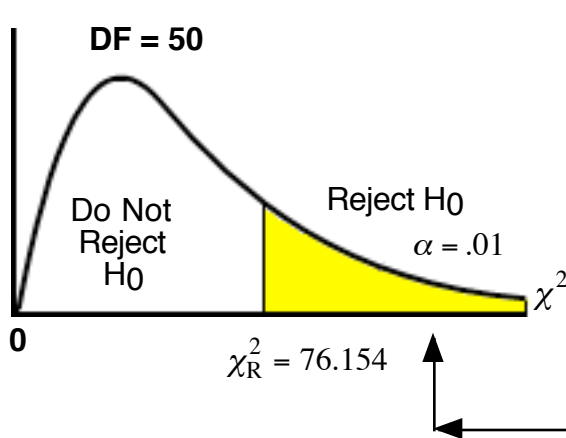
$H_1: \sigma > 250$ (One Tail Test, Right Tail)

Population Standard Deviation: $\sigma = 250$

$n = 51$ $\alpha = .01$ (all .01 in the right tail)

Graph of Critical information:

Test Statistic:



$$\chi^2 = \frac{(n-1)s_x^2}{\sigma^2}$$

$$\chi^2 = \frac{(51-1)315^2}{250^2}$$

$$\chi^2 = 79.38$$

Conclusion based on H_0 : Reject H_0

Conclusion based on the problem:

There is sufficient evidence at the $\alpha = .01$ level **to support the claim** that the standard deviation in the rent of two bedroom apartments is **more than \$ 250**.

| Chi-Square Distribution: Critical Values | | | | | | | | | | |
|--|------------------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| | Area in the Right Tail | | | | | | | | | |
| D of F | 0.995 | 0.99 | 0.975 | 0.95 | 0.9 | 0.10 | 0.05 | 0.025 | 0.01 | 0.005 |
| 50 | 27.991 | 29.707 | 32.357 | 34.764 | 37.689 | 63.167 | 67.505 | 71.420 | 76.154 | 79.490 |

Testing a Claim About the Population Standard Deviation Example 2 (One Tail Left Tail Test)

The Film Producers Guild reports that the average length of motion pictures is 105 minutes with a standard deviation of 10 minutes. A film studies class refutes that and claims that the standard deviation is less than 10 minutes. They **select 81 movies at random** and find that the **average length is 103 minutes** with a **standard deviation of 9 minutes**. Test the claim at a **.05 significance level** that the standard deviation in the length of movies is **less than 10 minutes**. Assume that **the population is normal**.

$$H_0: \sigma = 10$$

$$\text{Sample Standard deviation: } s_x = 9$$

$$H_1: \sigma < 10 \text{ (One Tail Test, Left Tail)}$$

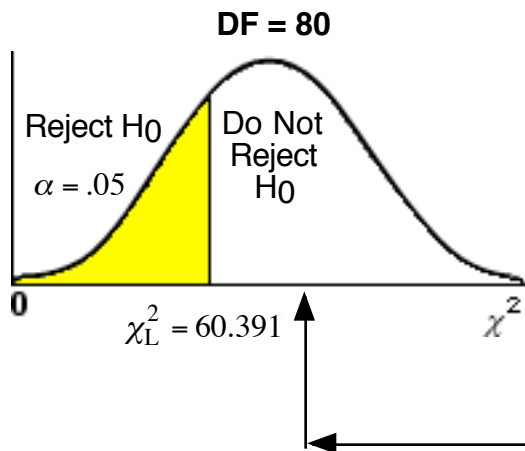
$$\text{Population Standard deviation: } \sigma = 10$$

$$n = 81$$

$$\alpha = .05 \text{ (all .05 in the left tail)}$$

Graph of Critical information:

Test Statistic:



$$\chi^2 = \frac{(n-1)s_x^2}{\sigma^2}$$

$$\chi^2 = \frac{(81-1)9^2}{10^2}$$

$$\chi^2 = 64.8$$

Conclusion based on H_0 : Do Not Reject H_0

Conclusion based on the problem:

There is **not sufficient evidence** at the $\alpha = .05$ level to **reject** the hypothesis that the standard deviation in the length of movies is **equal to 10 minutes**.

or

There is **not sufficient evidence** at the $\alpha = .05$ level to **support** the claim that the standard deviation in the length of movies is **less than 10 minutes**.

| Chi-Square Distribution: Critical Values | | | | | | | | | | |
|--|------------------------|--------|--------|---------------|--------|--------|---------|---------|---------|---------|
| | Area in the Right Tail | | | | | | | | | |
| D of F | 0.995 | 0.99 | 0.975 | 0.95 | 0.9 | 0.10 | 0.05 | 0.025 | 0.01 | 0.005 |
| 80 | 51.172 | 53.540 | 57.153 | 60.391 | 64.278 | 96.578 | 101.879 | 106.629 | 112.329 | 116.321 |

Testing a Claim About the Population Standard Deviation Example 3 (Two Tail Test)

A local high school student feels that the 20 ounce Sprite bottles vary a lot from the listed 20 ounces. The local Sprite distributor tells the students that the average volume for these bottles is 20.3 ounces with a standard deviation of 1.5 ounces based on information from the parent company Coca Cola. The student **selects 41** 20 ounces bottles of Sprite at random from a local grocery store. The student finds that the **average volume of the 41 samples is 20.1** with a **standard deviation of 1.3** ounces. Test the claim at a **.05 significance level** that **the standard deviation of 20 ounces of sprite is not equal to 1.5 ounces**. Assume that **the population is normal**.

$$H_0: \sigma = 1.5$$

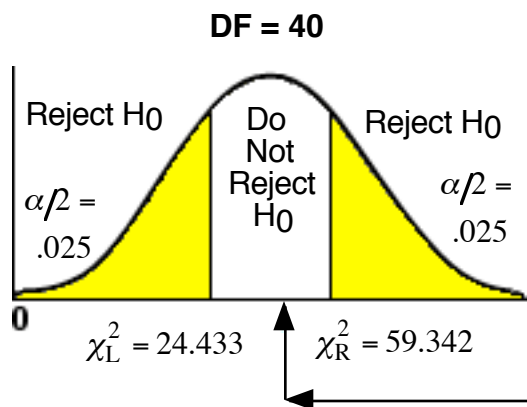
$$\text{Sample Standard deviation: } s_x = 1.3$$

$$H_1: \sigma \neq 1.5 \text{ (Two Tail Test)}$$

$$\text{Population Standard deviation: } \sigma = 1.5$$

$$n = 41 \quad \alpha = .05 \quad (\alpha/2 = .025 \text{ in each tail})$$

Graph of Critical information:



Test Statistic:

$$\chi^2 = \frac{(n-1)s_x^2}{\sigma^2}$$

$$\chi^2 = \frac{(41-1)1.3^2}{1.5^2}$$

$$\chi^2 = 30.04$$

Conclusion based on H_0 : Do not Reject H_0

Conclusion based on the problem:

There is **not sufficient evidence** at the $\alpha = .05$ level to **reject the hypothesis** that the standard deviation of 20 ounces of sprite is **equal to 1.5 ounces**.

or

There is **not sufficient evidence** at the $\alpha = .05$ level to **support** the claim that the standard deviation of 20 ounces of sprite is **not equal to 1.5 ounces**.

| Chi-Square Distribution: Critical Values | | | | | | | | | | |
|--|------------------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| | Area in the Right Tail | | | | | | | | | |
| D of F | 0.995 | 0.99 | 0.975 | 0.95 | 0.9 | 0.10 | 0.05 | 0.025 | 0.01 | 0.005 |
| 40 | 20.707 | 21.164 | 24.433 | 26.509 | 29.051 | 51.805 | 55.758 | 59.342 | 63.691 | 66.766 |